## A short course on

# Equilibrium 

This video:<br>Determinate Structures

Terje's Toolbox is freely available at terje.civil.ubc.ca

# Analysis of Determinate Structures 

What is analysis?

What is determinate?

What is a structure?

## A Structure is...

- Comprised of "longitudinal" members
- With a cross-section $工$

- Truss?
- Beam?

- Frame?
- Mixed?



## Analysis is...

Structural engineering = Design + Analysis

Design = Establish trial dimensions

Analysis $=$ Determine deformations and internal forces due to external loads

BMD = Bending moment diagram
SFD = Shear force diagram
AFD = Axial force diagram

## Internal Forces



Bending moment diagram, BMD


Shear force diagram, SFD

Axial force, N


## Determinacy is...

## Degree of static indeterminacy (DSI)

DSI = number of unknown forces in the structure - number of equilibrium equations
DSI=0 means determinate

DSI=0 means equilibrium is sufficient to determine BMD, SFD, AFD

We consider only determinate structures in this video

Compute DSI in the course on indeterminate structures

## Determinacy also means...

Equilibrium is sufficient

No need to know material behaviour to find forces

Stiffness of the structure does not influence the distribution of forces in the structure

Will NOT have additional forces due to support settlements or temperature changes

Does not possess redundancy

Structure will collapse if one member or one support fails

## Conventions



## BMD, SFD, AFD

Diagrams drawn along members, showing what occurs inside the member

> AFD in truss or frame members
> Tension is positive or negative?

BMD in beam and frame members
Use signs, or draw the diagram on a specified side of the member?

SFD in beam and frame members
Use signs, or draw the diagram on a specified side of the member?

## Choices Made



Bending moment diagram, BMD


Axial force diagram, AFD


BMDs are drawn on the tension side without signs

SFDs are drawn on either side of the member, but marked with a sign that indicates clockwise (+) or counter-clockwise (-) shear force

AFDs are drawn on either side of the member, but marked with a sign that indicates tension (+) or compression (-)

## Truss

- Determine reaction forces

- Select an arbitrary joint with maximum two unknown forces
- Use "equilibrium of forces at a point" to determine the unknown forces there
- Go to the next joint...


## Beam/Frame

- Determine reactions
- Determine bending moment at key locations

- Draw the BMD between those locations:

| Load: | None | Uniform | Linear | etc. |
| ---: | :--- | :--- | :--- | :--- |
| Bending moment: | Linear | Parabola | 3rd order | etc. |

- Obtain SFD from BMD (beam equations)
- Obtain AFD from SFD (equilibrium at a point) $\}$ Good to know because advanced methods give end moments


## Beam Equations



## Integration



$$
V=\int q d x=q \cdot x
$$

Shear force at base ( $x=L$ ): $V=q L$

$$
M=\int V d x=\int q \cdot x d x=\frac{q x^{2}}{2}
$$

Bending moment at base $(x=L): M=q L^{2} / 2$

## Formulas to Remember



## Reactions First?

## To be safe, yes...

but sometimes life is easier...


More lectures:

Terje's Toobox:
terje.civil.ubc.ca

