

A short course on

# Equilibrium

This video:

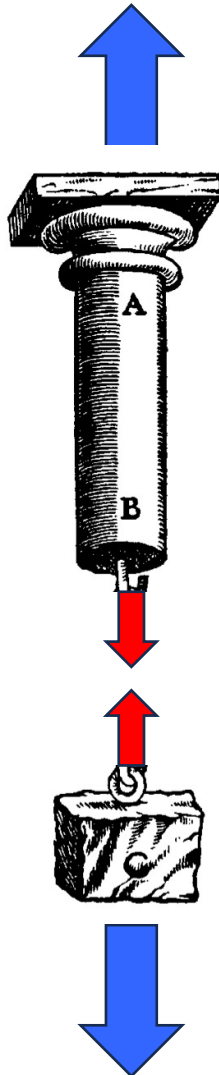
**Forces and Moments**

Terje's Toolbox is freely available at [terje.civil.ubc.ca](http://terje.civil.ubc.ca)

It is created and maintained by Professor Terje Haukaas, Ph.D., P.Eng.,  
Department of Civil Engineering, The University of British Columbia (UBC), Vancouver, Canada

# Balance of Forces

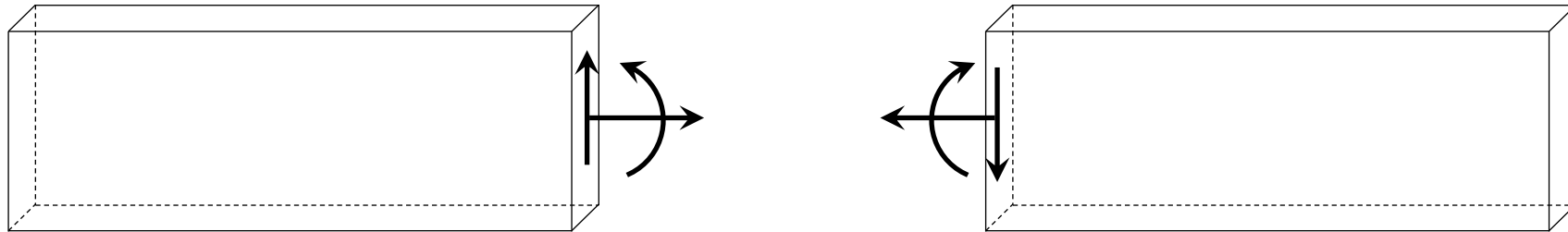
Galileo (1638)



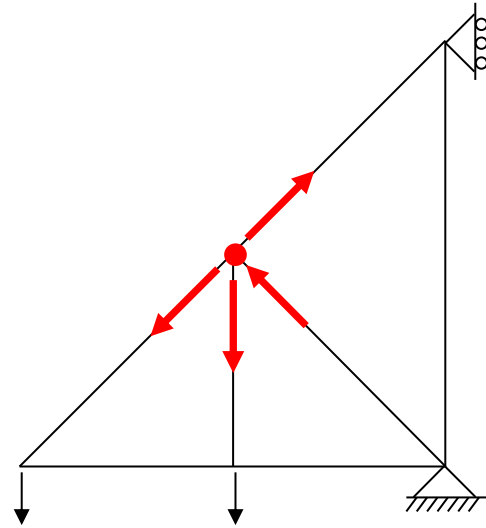
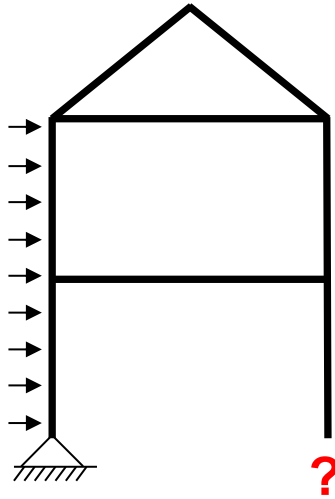
Newton (1687)

1. A body remains at rest, or in motion at a constant speed in a straight line, unless acted upon by a force
2. When a body is acted upon by a force, the time rate of change of its momentum equals the force
3. If two bodies exert forces on each other, these forces have the same magnitude but opposite directions

# Equal & Opposite

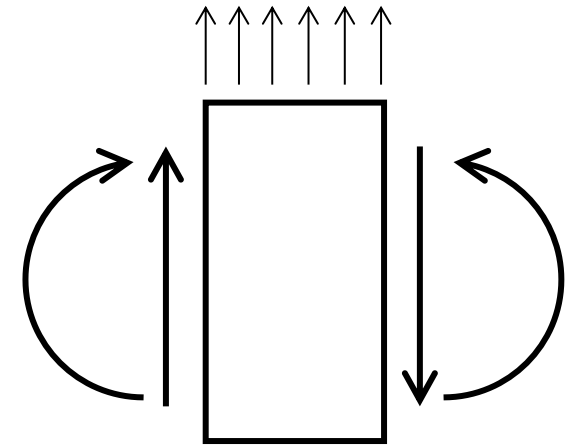
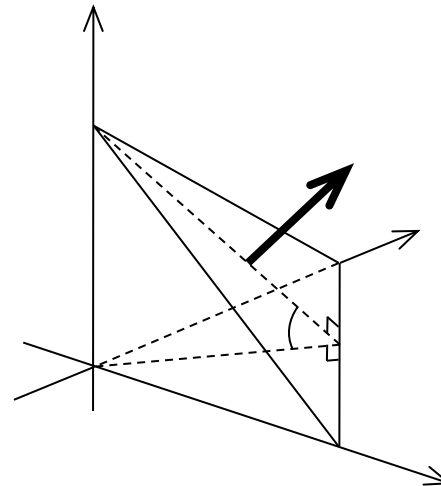
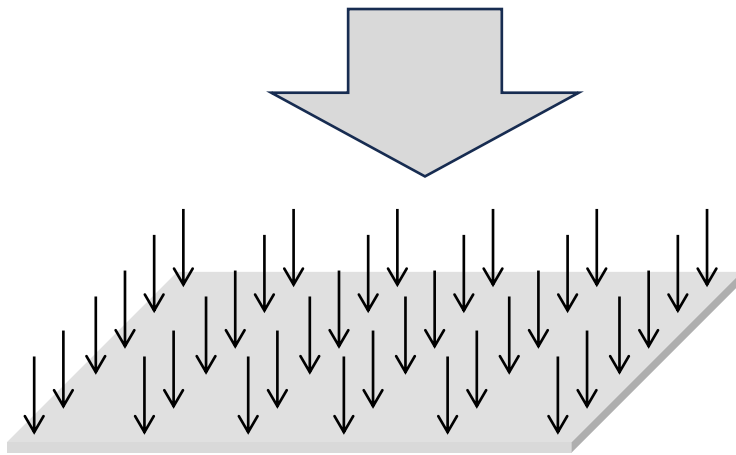


# Equilibrium is Always Important

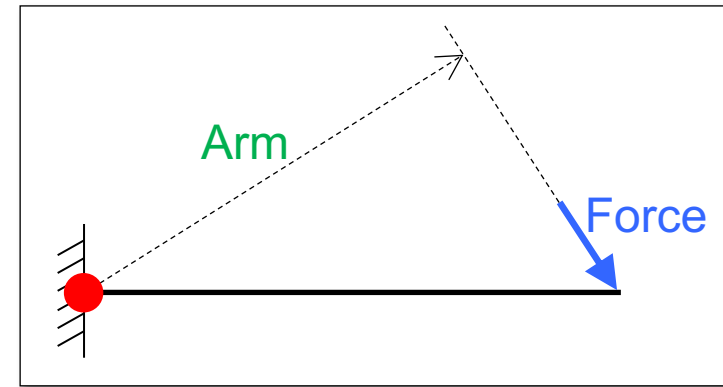
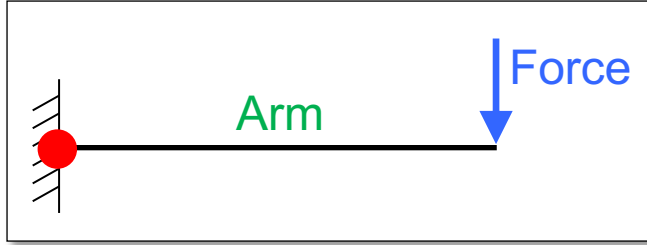


$$\int \sigma \cdot \delta \varepsilon = \delta W_{\text{ext}}$$

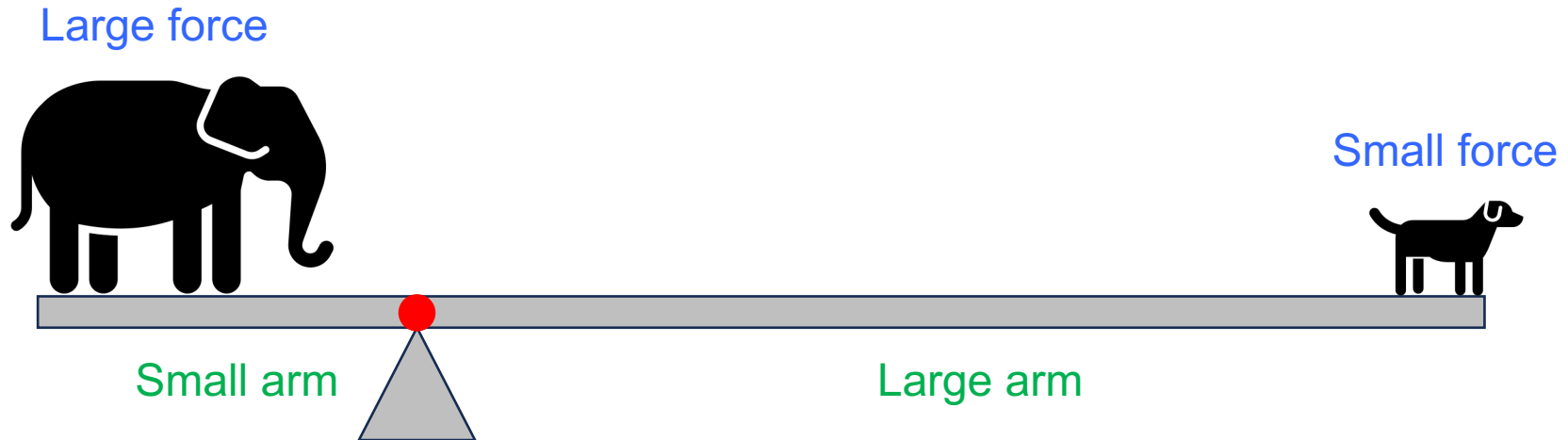
$$\mathbf{Ku} = \mathbf{F}$$



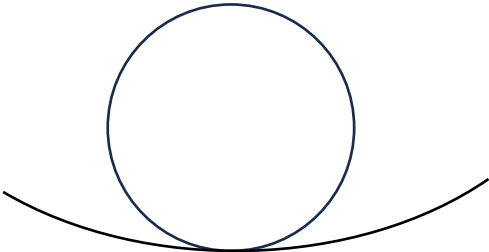
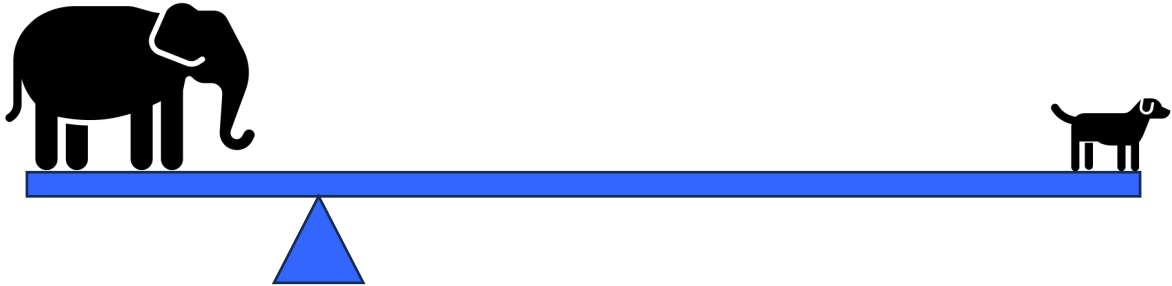
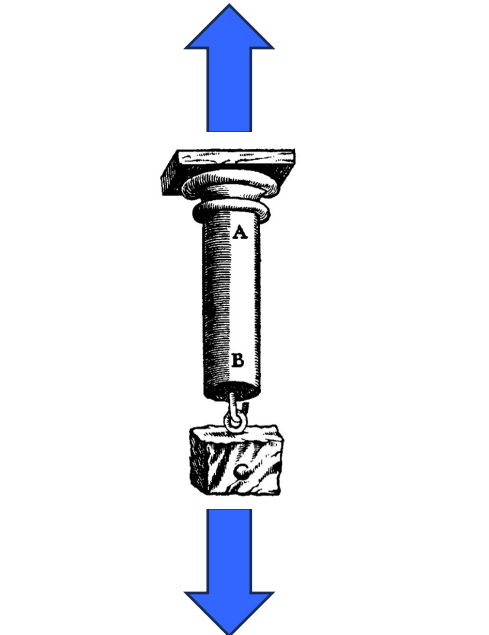
# Balance of Moments



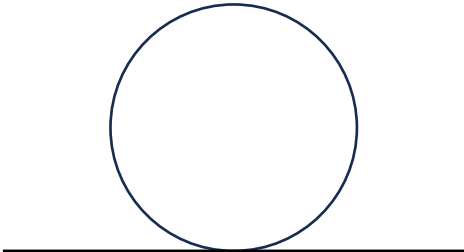
$$\text{Moment} = \text{Force} \cdot \text{Arm}$$



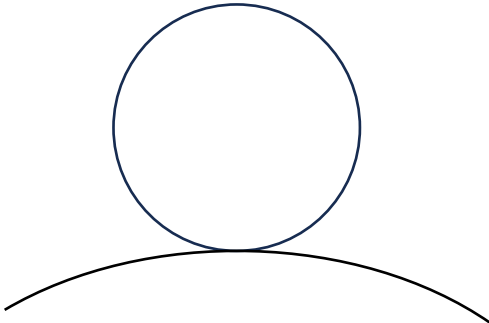
# Types of Equilibrium



Stable



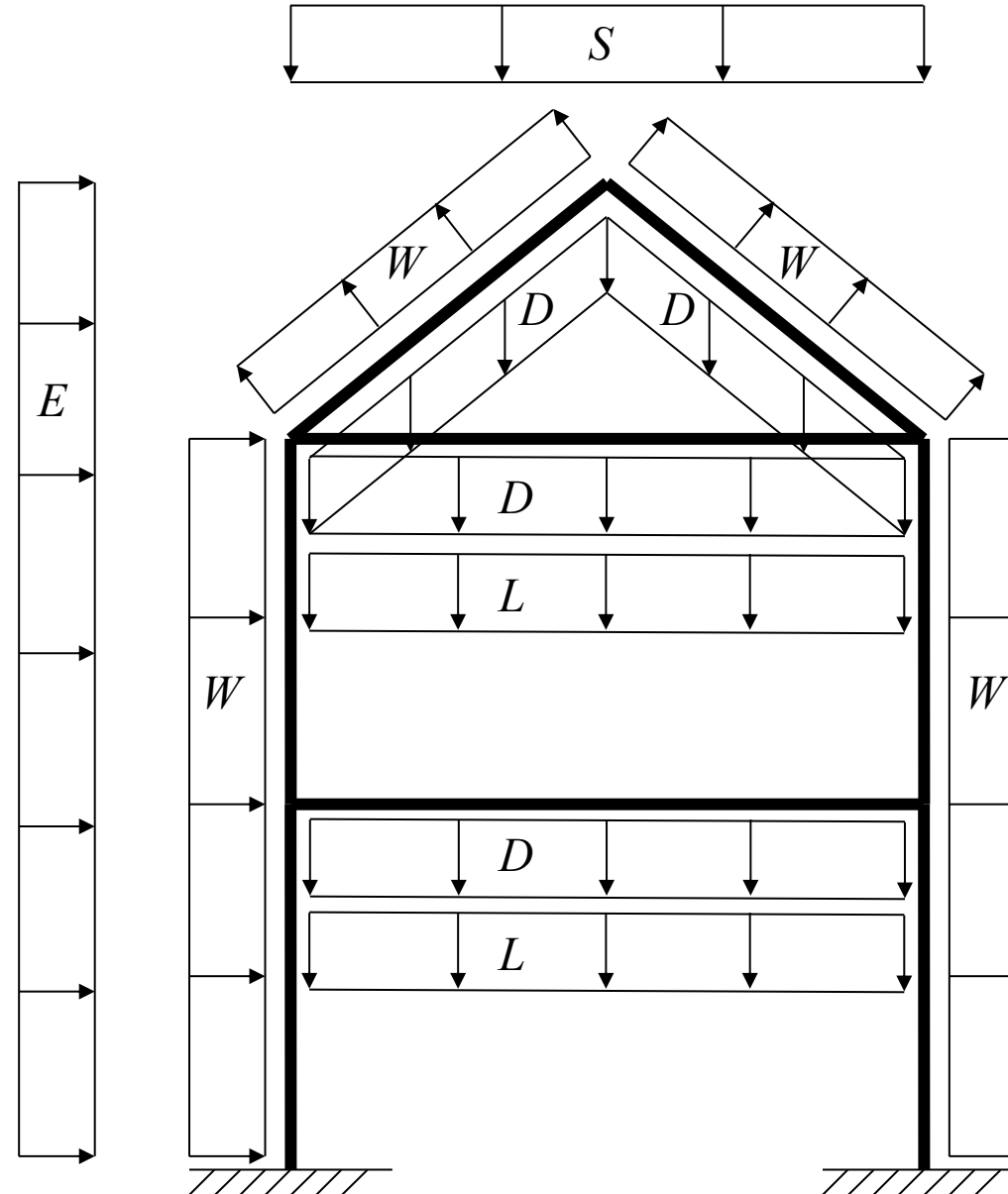
Neutral



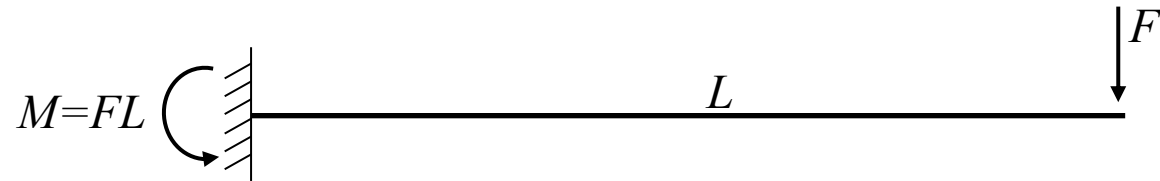
Unstable

# Forces on Structures

- $S$  = snow
- $W$  = wind
- $D$  = dead load
- $L$  = live load
- $E$  = earthquake

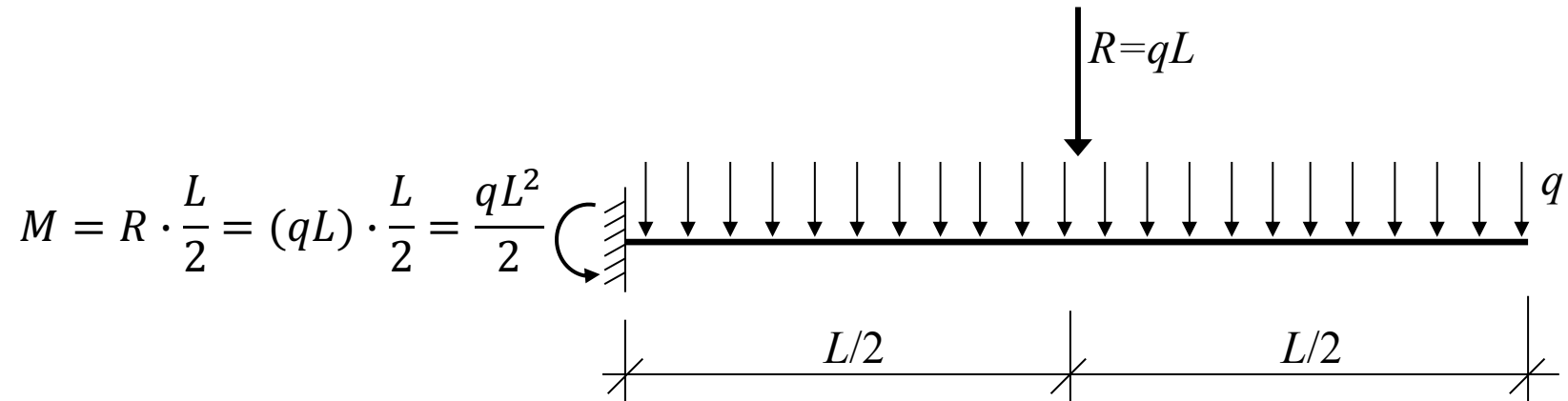


# Force $\rightarrow$ Moment

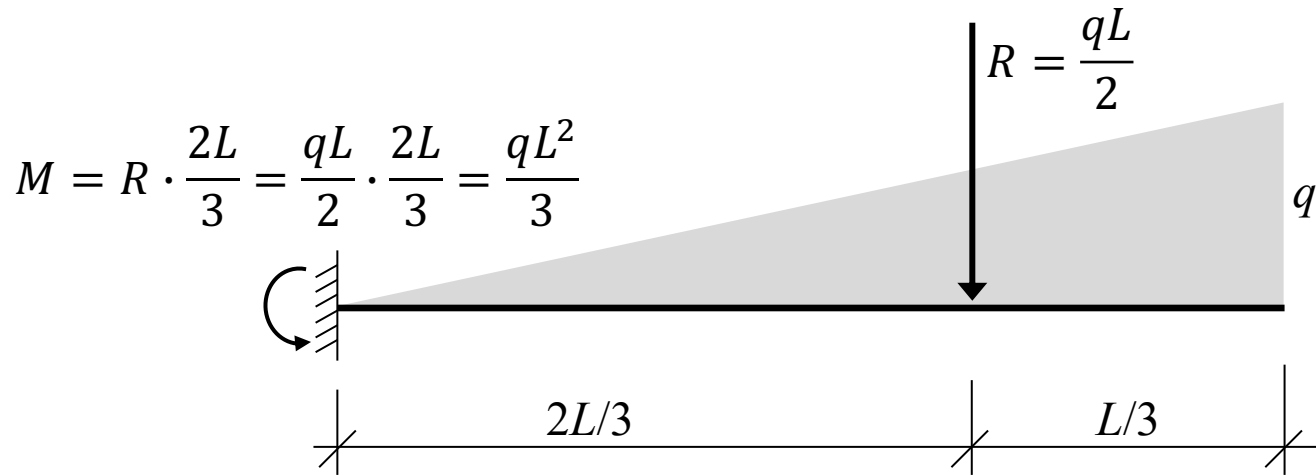




# Distributed Load $\rightarrow$ Force $\rightarrow$ Moment

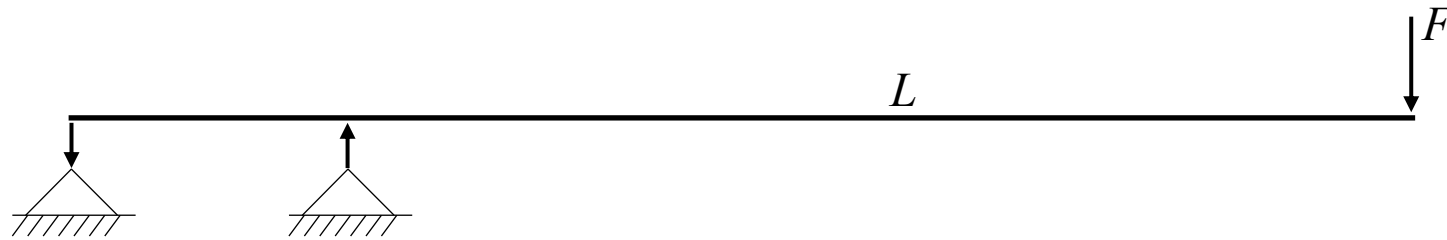


# Beyond Uniform Load

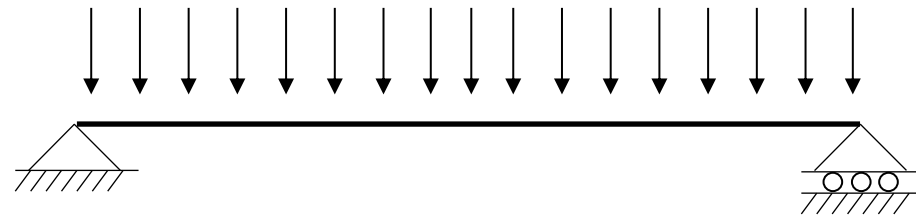
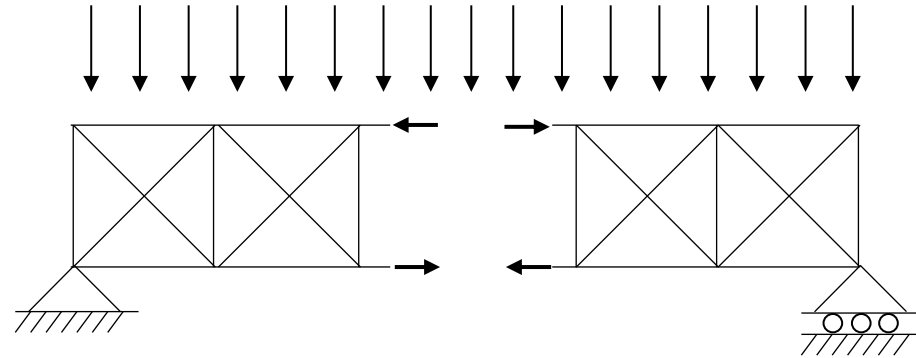


Shapes with length $L$	Area	Centroid location
	$A = \frac{h \cdot L}{2}$	$\bar{x} = \frac{L}{3}$
	$A = \frac{h \cdot L}{3}$	$\bar{x} = \frac{L}{4}$
	$A = \frac{2 \cdot h \cdot L}{3}$	$\bar{x} = \frac{3L}{8}$

# Moment $\rightarrow$ Force Pair



# Moment $\rightarrow$ Force Pair



More lectures:

Terje's Toolbox:

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